Three regulars share a p(o)int

In the following figure the quadrilateral, the pentagon and the hexagon are all regular. Given that the ratio of a pentagon diagonal to a side is $\frac{1+\sqrt{5}}{2}$, show that the shaded triangle is isosceles.