### 4.3.6 Duals by the midpoint construction

In the section Dual polygons we obtained a dual via an intermediate circle. Another way is to take as vertices of quadrilateral $X$ the side midpoints of quadrilateral $Y$. This gives a parallelogram in all cases, the Varignon parallelogram. An interesting duality exists between the equidiagonal quadrilateral and the orthodiagonal quadrilateral.

A quadrilateral is equidiagonal if and only if the Varignon parallelogram is orthodiagonal (a rhombus).
A quadrilateral is orthodiagonal if and only if the Varignon parallelogram is equidiagonal (a rectangle).


If a quadrilateral is both ortho- and equidiagonal, the Varignon parallelogram must be both a rhombus and a rectangle, that is, a square.

